Power Supplies for TESLA Modulators
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DESY
TESLA 2000-36
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1 Introduction

Modulators are used to generate the pulsed power for the klystrons of the superconducting linear accelerator TESLA. They produce rectangular high voltage pulses of up to 120 kV. The electrical power during the pulse is typically 15 MW and can be at maximum 16.8 MW. The pulse length is 1.7 ms with a repetition rate of 5 Hz, for app. 10% of the modulators it is 10 Hz. This leads to a needed pulsed power of 8.9 GW. It is obvious that this energy can not be taken from the mains directly. Therefore it is stored in capacitor banks to be released during the pulse. Power supplies are needed to recharge the capacitor banks and to decouple the low repetition rate from the mains.

2 Bouncer modulator

Beside other designs the bouncer modulator is the most promising solution for the modulators in respect to cost and ease of design. Fig. 1 shows the principle schematic with the main capacitor bank, a semiconductor switch, the pulse transformer, the bouncer circuit and the HV power supply. For safety reasons ignitrons are installed to quick discharge the main capacitor bank in case of failure in the klystron.

![Principle schematic of the bouncer modulator](image)

The specification for the modulators are

<table>
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<th>Parameter</th>
<th>Typical</th>
<th>Maximum</th>
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<tr>
<td>Klystron gun voltage</td>
<td>115 kV</td>
<td>120 kV</td>
</tr>
<tr>
<td>Klystron gun current</td>
<td>130 A</td>
<td>140 A</td>
</tr>
<tr>
<td>Electrical power</td>
<td>14.95 MW</td>
<td>16.8 MW</td>
</tr>
<tr>
<td>High voltage pulse duration</td>
<td>&lt; 1.7 ms</td>
<td>1.7 ms</td>
</tr>
<tr>
<td>High voltage rise time (0 to 99%)</td>
<td>&lt; 0.2 ms</td>
<td>0.2 ms</td>
</tr>
<tr>
<td>Pulse to pulse voltage fluctuation</td>
<td>&lt; +/- 0.5%</td>
<td>+/- 0.5%</td>
</tr>
<tr>
<td>Pulse flatness during flat top</td>
<td>&lt; +/- 0.5%</td>
<td>+/- 0.5%</td>
</tr>
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To generate the HV pulses the main capacitor bank is charged to a voltage at the 10 kV level. Via the semiconductor switch the pulse transformer is connected to the cap bank. With the step up ratio of 1:12 the voltage is transformed to the 120 kV level. During the pulse the voltage of the main capacitor droops about 19%. The principle can be seen in Fig. 2. To correct the voltage droop to +/- 0.5% a bouncer circuit is used. This is a resonant LC circuit which creates a low frequency sine wave which is triggered slightly
before the main pulse. The main pulse is positioned in the linear part of this sine wave. The sum of both voltages is a rectangular voltage of the desired parameters. With the use of the bouncer the stored energy inside the modulator is decreased.

Fig. 2: Voltage curve form of the main capacitor bank in the modulator

3 High voltage power supply

There will be a power supply for each modulator. It will have a standard 400 V three phase input. The output voltage will be 12 kV DC. The nominal power will be 150 kW for the 5 Hz and 300 kW for the 10 Hz repetition rate. The typical power needed for the 5 Hz operation is 120 kW. The power supplies will be built in modules. By this a high reliability and a good maintainability is given. The power supply cabinet is connected to the cabinet of the modulator. The size of the power supply will be 1.2m * 1.6m* 2m (l*w*h)

The advantages of having one power supply per modulator are:

- very high redundancy in the rf system. A failure of a modulator or a power supply does not affect any other modulator
- a failure in a single power supply module will not turn down the modulator
- each power supply can be regulated independently with a high regulation dynamic
- at the low voltage level switch gear is available as low price commercial of the shelf component.
- in case of replacing or working at the power supplies no further high voltage safety requirements are given

During operation the power supply has to meet two requirements:

- The main capacitor bank has to be recharged to an accurate value of voltage in order to obtain the same voltage at the klystron from pulse to pulse. The accuracy has to be +/- 0.5 %.
- The low repetition rates of 5 Hz and 10 Hz have to be suppressed in order not to produce disturbances to the mains.
4 Disturbances to the mains

4.1 Pulsed power of the modulators

In the main linac 560 modulators are in operation. For the injectors another 24 are installed leading to a total sum of 584 modulators in operation. There are another 12 modulators in the main linac in stand by mode ready to start operation in case of a failure of the working units. 519 modulators operate with the 5 Hz repetition rate. The other 65 modulators will have a repetition rate of 10 Hz. This leads to a typical total peak pulse power of 8.8 GW at 5 Hz repetition rate1 GW for the intermediate pulses at 10 Hz repetition rate. This power is taken during 1.7 ms. During 200 ms respecting 100 ms the energy taken from the capacitors has to be recharged without disturbing the mains.

4.2 Allowed distortions to the mains

The German standard VDE 0838 or the equivalent European standard EN 61000 defines the amount of distortions that are allowed to be produced by a consumer of electrical energy. These distortions are defined as relative voltage changes d with

\[ d = \frac{\Delta U}{U} = \frac{\Delta S}{S_{sc}} \]

\( d \) = allowed relative voltage changes
\( U \) = mains voltage
\( \Delta U \) = variation of mains voltage
\( \Delta S \) = variation of power due to the modulators
\( S_{sc} \) = short circuit power of the mains

In general no consumer of electrical energy is allowed to produce more than 3 % of voltage variation to the public mains. For low repetitive changes below 25 Hz this value is even more decreased. Voltage changes below 25 Hz are seen as changes in the luminance of the electric light. Since the human eye is very sensitive to these changes this appears as flickering light. These frequencies are called flicker frequencies.

The value \( d \) for TESLA can be taken from the diagram in Fig. 3. The value \( r \) is the number of voltage changes within one minute.

\[ r \text{ (min}^{-1}) = 5 \text{ [s}^{-1}] \times 2 \times 60 \text{ s} = 600 \]

For this value \( d \) is \(< 0.5\%\).

TESLA will have a distributed electrical power supply system with a voltage of 20 kV. With the short circuit power \( S_{sc} \) of app. 200MVA per service hall the allowed power variation can be calculated to:

\[ \Delta S < 200\text{MVA} \times 0.005 = 1\text{MVA} \]

In each service hall up to 100 modulators are to be installed. The typical real power consumption is assumed to 15 MW per hall. Therefore each modulator shall not produce more the 10 kVA variation over the entire time between the pulses. With a nominal input power of 150
kW this leads to an allowed variation of 6.5 % of this value including the reactive power changes.

For the 10 Hz operation the curve of relative voltage changes has a minimum. The allowed voltage variation is decreased to $d = 0.25 \%$. The number of modulators working at the 10 Hz level is low. There are 55 modulators installed in the service hall on the DESY site. The power supplies have an allowed variation of 3 % of their nominal power respecting 3.75% of the typical power. The remaining 10 power supplies are installed in another service hall having a separate mains connection point.

Fig. 3: Compatibility of regular repetitive rectangular voltage changes

## 5 Types of power supplies

The given definition of the allowed distortions to the mains makes it impossible to use a variety of topologies of power supplies. The power supply used in the first prototypes of the modulators at TESLA Test Facility are primary regulated SCR bridges with transformer and secondary diode bridge. This can not be used for TESLA due to the large variation in reactive power. Three phase rectifiers using SCRs like B6 bridges cannot be used for the same reason. Switched mode power supplies in the needed power and voltage range have recently come to the market and are available from industry.

Among other solutions described in [1,9] the following topologies have been investigated at DESY.

1) Series resonance sine converter
2) Series connection of buck converters
3) Hybrid power supply
4) SCR bridges in series with a diode rectifier
5.1 Series resonance sine converter

The power supply shown in Fig. 4 was developed at DESY. This topology is known for small power supplies for auxiliary voltages. So far it has not been used as power supply to charge large capacitive loads in a constant power mode.

![Equivalent Circuit Diagram](image)

The equivalent circuit according to the arithmetic average of the supply current $I_B$:

$$ R = \frac{T}{C} $$

Fig. 5: Equivalent circuit of the power supply

The equivalent circuit of the switch mode power supply is a resistor $R$ which is constant when the period time $T$ of the switching frequency $f$ (10 – 20 kHz) is constant. This resistance is independent of the capacitor voltage $U_{Cloud}$ and the pulse repetition rate of the modulator. By this the input power is (in a wide range) independent from the voltage of the main capacitor bank of the modulator.

To describe the function of the power supply Fig. 6 is used.

Assumption: $u_c=0V$, $I_L=0A$ and $S_1$ turning on

Because of the stray inductance $L$ of the transformer the current $i_L$ keeps zero while turning $S_1$ on (zero current switching power supply). Then the current $i_L$ raises and the resonance capacitor $C$ is charged. While charging the resonance capacitor $C$ the supply current $I_B$ is equivalent to the resonance capacitor current $i_L$.

When the resonance capacitor voltage $u_C$ reaches the supply voltage $U_B$ diode $D_1$ will start to conduct. The current $i_L$ continues flowing forced by the energy stored in the stray inductance $L$ of the transformer. Since the path of the current $i_L$ is no longer through the resonance capacitor $C$ and the supply current $I_B$ equals zero.
The energy stored in the stray inductance $L$ of the transformer will slowly be passed to the load $C_{\text{load}}$ and the current $i_L$ decreases linearly to zero.

After that a new cycle can start by turning $S_1$ off and $S_2$ on. The corresponding voltage and current waveforms can be seen in Fig. 8. With each loading and unloading period the same amount of energy is transmitted from the primary side of the transformer to the main capacitor bank. This amount is the energy of the resonance capacitor loaded to the voltage $U_B$ or unloaded to 0.

Fig. 6: Series resonance sine converter with only one capacitor

Fig. 7: Voltage and current functions of the half-bridge

Please note that the current pulses are in the range of 20 kHz. They are filtered by the input filter and do not pass to the mains.

Derivation of the arithmetic average supply current $I_B$:
While charging the resonance capacitor $C$ the supply current $i_B$ is equivalent to the resonance capacitor current $i_L$. Therefore the charge $Q$ taken from the power supply to the resonance capacitor $C$ equals $Q = CU_B$.

The charge $Q$ can also be expressed as follows:

$$Q = \int_{0}^{T} i_B \, \text{dt} = CU_B$$

Multiplication of the integral with the term $\frac{T}{T}$ with $T =$ period time of the switching time:

$$Q = T \times \left[ \frac{1}{T} \int_{0}^{T} i_B \, \text{dt} \right] = CU_B$$

The term in brackets is equivalent to the average supply current $I_B = \frac{1}{T} \int_{0}^{T} i_B \, \text{dt}$.

$$Q = T \times I_B = CU_B$$

The resulting expression for the average supply current is:

$$I_B = \frac{CU_B}{T} = \frac{U_B}{R} \quad \text{with} \quad R = \frac{T}{C}$$

The voltage and current wave forms for the half bridge shown in Fig 4 are given in Fig 8. The same principle as for the half bridge is valid. The difference is that the frequency of the current is doubled and the currents are decreased. When one of the capacitors is loaded, the second capacitor is unloading and vice versa.

Fig 8: Voltage and current waveforms of power supply Fig. 4

The required power is with today’s technique hard to fulfill with just one power part. A 300 kW prototype consisting of four modules having 75 kW each is going to be tested in TTF. One 75 kW module was tested successfully.
5.2 Buck converter
To achieve the high voltage level of the main capacitor bank it is possible to stack a group of low voltage power supplies. This topology is used for power supplies that manufactured in industry. The units are now under construction an will be used for some of the TTF modulators. The power supplies are buck converters each having a nominal voltage of app. 750V each. 16 modules are stacked to deliver the required voltage of 12 kV. The transformer has a 400 V input and 16 outputs of which 8 outputs are in delta, the other 8 outputs are in star to get less mains harmonics. Fig. 9 shows the principle diagram of such a power supply.

Fig. 9: Power supplies with stacked buck converters

The buck converters are working with a Pulse Width Modulation (PWM). The overlaid regulation for the voltage and the constant input power is accomplished on an external board that is developed and provided by DESY. The internal regulation of the power supply is a power regulation. The units will receive the power reference signal from the DESY regulation and transforms this into voltage and current values.

5.3 Hybrid power supply
When looking at the development in cost of switched mode power supplies a permanent decrease can be seen. In the last 5 to 10 years the prices have been reduced by a factor of two. Nevertheless they are still high in comparison with SCR or diode technology. Therefore another solution is considered. This is the hybrid power supply. (Fig 10)
5.4 SCR supply with diode rectifier

The same basic idea as for the hybrid supply is assumed. Here the switched mode supply shall be replaced by SCR technology to further reduce cost. The voltage of the diode rectifier is at 10 kV. The SCR has to be in inverter mode at the beginning of the loading period to decrease the voltage. At the end of the loading period the power supply has to add voltage. shows A principle schematic is shown in Fig. 12. The voltage curves are shown in Fig. 13.
Here two versions are possible:

- The SCR power supply has a single phase angle control
- The SCR power supply is driven in sequential phase control

Both solutions have to take care for the reactive power of the SCR supply in order to keep the distortions of the mains low.

### 5.4.1 SCR bridge with single phase control

The power of the SCR supply can be calculated:

\[
P = U_{di} \cdot I_U \cdot \cos \alpha
\]

\[
Q = \sqrt{Q_1^2 + Q_0^2}
\]

\[
S = \sqrt{P^2 + Q^2}
\]

\[
Q_1 = U_{di} \cdot I_U \cdot \sin \alpha
\]

\[
S_1 = U_{di} \cdot I_U
\]

\[
Q_0 = 0.31 \cdot U_{di} \cdot I_U
\]

The correspondence of the reactive power to the real power in dependence of the trigger angle is shown in Fig. 14.

![Fig. 14: Real and reactive power in dependence of the phase angle \(\alpha\)](image)

The overall real power is:

\[
P = P_{\text{thyristor}} + P_{\text{diode}} = U_{di} \cdot I_U \cdot \cos \alpha + U_d \cdot I_U.
\]

For a constant power \(\alpha\) can be calculated:

\[
\alpha = \arccos \left( \frac{P}{I_U} - U_{di} \right) \cdot \frac{1}{U_{di}}
\]

The arccos function is only valid when \(\frac{P}{I_U} - U_{di} \cdot \frac{1}{U_{di}}\) is between –1 and 1.

If the relation

\[
\frac{P}{U_{di} + U_{do}} \leq I_U \leq \frac{P}{U_{di} - U_{do}}
\]
is not valid, no phase shift angles can be calculated for a constant power mode.

The simulation shows that a constant power mode is possible when having a nominal voltage of 3 kV of the SCR supply. The power diagram is shown in Fig. 15. The power was calculated in periods of 20 ms the repetition rate is 10 Hz.

![Power Diagram](image)

**Fig.15:** Power diagram of a series connection of a diode and SCR bridge \( \alpha(P) \)

### 5.4.2 SCR bridge with sequential phase control

In literature the half regulated B6 bridge can be found as topology to produce low reactive power. In the B6 bridge either the anode or the cathode SCRs are replaced by diodes depending whether the rectifier mode or the inverter mode is driven. When using SCRs instead of diodes and varying both phase angle it is possible to regulate the reactive power in the region between half controlled bridge and full controlled bridge. This type of regulation is controlled sequential phase control. The real/reactive power diagram is shown in Fig. 16. The simulation results are shown in Fig. 17.

The formulas to calculate the power are:

\[
\begin{align*}
P &= \frac{U_{di}}{2} \cdot I_L \cdot (\cos \alpha_1 + \cos \alpha_2) \\
Q &= \sqrt{Q_1^2 + Q_o^2} \\
S &= \sqrt{P^2 + Q^2} \\
Q_1 &= \frac{U_{di}}{2} \cdot I_L \cdot (\sin \alpha_1 + \sin \alpha_2) \\
S_1 &= U_{di} \cdot I_L \\
Qo &= 0,31 \cdot U_{di} \cdot I_L
\end{align*}
\]

P: real power  
Q: reactive power  
S: apparent power  
Q_1: fundamental reactive power  
Qo: harmonics reactive power  
S_1: fundamental apparent power
The total power can be calculated with
\[ P = P_{\text{diode}} + P_{\text{thyristor}}(\alpha_1, \alpha_2) \]
\[ Q = Q_{\text{diode}} + P_{\text{thyristor}}(\alpha_1, \alpha_2) \]

With
\[
P = U_{\text{diode}} \cdot \frac{I_t}{2} \cdot (\cos \alpha_1 + \cos \alpha_2) + U_{\text{did}} \cdot I_t.
\]
\[
Q = \sqrt{(U_{\text{diag}} \cdot \frac{I_t}{2} \cdot (\sin \alpha_1 + \sin \alpha_2))^2 + (0,31 \cdot U_{\text{di}} \cdot I_t)^2 + 0,31 \cdot U_{\text{did}} \cdot I_t}
\]
\[
\cos \alpha_1 + \cos \alpha_2 = \frac{2 \cdot (P - U_{\text{did}} \cdot I_t)}{U_{\text{di}} \cdot I_t}
\]
\[
\sin \alpha_1 + \sin \alpha_2 = \sqrt{4 \cdot \left[ \frac{(Q - 0,31 \cdot U_{\text{did}} \cdot I_t)^2}{(U_{\text{di}} \cdot I_t)^2} - 0,31^2 \right]}
\]

In the simulation it is shown that the power supplies fulfill the requirements of low changes in apparent power nevertheless the regulation requires a lot of difficulty mathematics. Due to the arccos functions the values for \( \alpha, \alpha_1, \alpha_2 \) are defined only in a small area.
Both power supplies require a large filter choke to smooth the loading current. In spite of the very good price this type of power supply is not taken.
6 Regulation

The regulation is a major part of a constant power power supply. The voltage of the capacitor bank at the trigger time of the pulses has to have a pulse to pulse repetition accuracy of +/- 0.5%. This in combination with the demand of constant power requires a digital regulation. To be able to react on variations of the mains, temperature effects or non-linear behavior of components the regulation is self learning. A simplified modulator circuit is shown in Fig. 18.

![Fig. 18 Simplified modulator circuit](image)

6.1 Principle of regulation

The regulator contains a RAM wherein the charging curve of the capacitor voltage $U_{\text{Cloud}}$ is stored. It is driven according to the RAM curve. A fast regulator ensures that the RAM curve and the capacitor voltage $U_{\text{Cloud}}$ are equal despite of even fast voltage variations of the mains voltage $U_{\text{MAINS}}$. For this reason it is obvious that the final voltage $U_{e} = U_{\text{Cloud}}$ at time $t_e$ remains the same at each charging cycle because it equals the well known RAM curve. Fig. 19 shows again the voltage curve of the main capacitor bank.

$$W_{\text{Cloud}} = \frac{1}{2} C_{\text{load}} * U_{\text{Cloud}}^2$$
For achieving constant input power a learning process is introduced. A voltage charging curve for $C_{\text{load}}$ is determined. With this curve the final charging voltage equals the nominal voltage ($V_{\text{capend}}=V_{\text{capendref}}$). This charging curve is stored in the memory. The possible starting curve is shown in Fig. 20.

With this reference charging curve the input power is not yet constant but looks e.g. like the curve shown in Fig. 21. The aim is to have a constant power. With the self learning algorithm the stored reference curve is modified in such a way that the reference values are increased or decreased until the input power is constant.

The result of the learning process is equal output voltage $U_{\text{Cloud}}=U_e=\text{constant}$ after each charging cycle $T$ and constant input power consumption $P_{\text{in}}=P_{\text{average}}=\text{constant}$.

6.1.1 Regulation with unit RAM curve

To be independent from changes in the charging time $T$ (changes in repetition rate) or the output voltage $U_e$ a unit curve is stored in the RAM. By this it is not necessary to relearn this curve in case of change. The unit charging curve is simply scaled to the real time and voltage axis.
To linearize the regulation the capacitor voltages are used as squared values. This is because the energy stored in the capacitor $C_{\text{Load}}$ is proportional to the squared capacitor voltage $U_{\text{Cloud}}^2$. The linearized curve is stored as RAM curve.

$$W_{\text{Cloud}} = \frac{1}{2} C_{\text{Load}} * U_{\text{Cloud}}^2$$

$U_{\text{Cloudref}}^2(t)$ (reference curve) is the linearized reference value of the squared capacitor voltage $U_{\text{Cloud}}^2(t)$ (actual curve).

The reference value $U_{\text{Cloudref}}^2$ and the linearized squared capacitor voltage $U_{\text{Cloud}}^2$ are passed to a P(I) regulator.

$$P_{\text{ref}} = K_p * (U_{\text{Cloudref}}^2 - U_{\text{Cloud}}^2)$$

The signal $P_{\text{ref}}$ is the signal steering the power consumption of the power supply (Fig.23). It is necessary that the actual input power $P_{\text{in}}$ is proportional to the steering signal $P_{\text{ref}}$ ($P_{\text{in}} \sim P_{\text{ref}}$). In some power supplies a pre-filter has to be used to ensure that $P_{\text{in}} \sim P_{\text{ref}}$. Droops of the mains voltage $U_{\text{MAINS}}$ are the most disturbing error signals for the P(I) regulator. The pre-filter in the proposed power supply for TESLA guarantees the independence of the input power $P_{\text{in}}$ from the mains voltage $U_{\text{MAINS}}$ ($P_{\text{ref}} \sim P_{\text{in}} \neq f(U_{\text{MAINS}})$).

The hardware of the regulation is based on a programmable ALTERA device. The device contains the complete regulation software, the pulse firing generation of the switched mode power supply and the interlocks for the power supply. The designed board is able to work in local mode. A VME interface allows to communicate with a control computer to feed in pre-calculated curve forms for the modulator. By this the learning time is decreased.
The regulation scheme is shown in Fig. 25.

Fig. 25: Block diagram of the self-learning regulation

7 Summary

Different types of power supplies are possible to fulfill the requirement of low disturbances to the mains. A switched mode power supply, the resonance converter was developed for the high voltage high power operation and successfully tested at DESY TTF. The next type of switched mode power supply used in TTF is a series connection of low voltage buck converters. As outlook for future power supplies with lower costs the hybrid power supply, a series connection of a diode bridge and a switched mode power supply, was investigated and give good results in simulation. A further cost reduction just using SCR technology is possible in simulation but has draw backs for real power supplies since the regulation is very complicated.

8 Literature

[1] Bothe, Pulse Generation for TESLA a Comparison of Various Methods, DESY print, TESLA 94-21
[3] VDE German standards